



**KERALA AGRICULTURAL UNIVERSITY**  
**B.Tech. (Ag. Engg.) 2017 Admission**  
**III Semester Final Examination-January-2019**

**Basc.2108**

**Engineering Mathematics-III (2+1)**

**Marks: 50**  
**Time: 2 hours**

**I Fill in the blanks:**

**(10x1=10)**

- 1 If  $\vec{A}$  is solenoidal then  $\text{div } \vec{A} =$  \_\_\_\_\_
- 2 The mapping  $w = \frac{1}{z}$  is known as \_\_\_\_\_
- 3 The poles of  $\frac{z+1}{z^2(z-2)}$  are \_\_\_\_\_
- 4 If  $f(x)$  is an even function then  $f(-x) =$  \_\_\_\_\_
- 5 If  $\vec{r}(t)$  is the position vector of a moving particle, then velocity is given by \_\_\_\_\_
- 6  $\nabla_x a \vec{f} =$  \_\_\_\_\_ (a is any scalar).
- 7 If the principal part of the Laurent's series expansion of  $f(z)$  about  $z = a$  has infinite number of terms then  $z = a$  is \_\_\_\_\_
- 8  $\int_{-c}^c f(z) dz =$  \_\_\_\_\_
- 9 The maximum of the modulus value of the directional derivative of the scalar function is-----
- 10  $\nabla(\vec{f} \cdot \vec{g}) =$  \_\_\_\_\_

**II Write Short notes on ANY FIVE of the following (5x2=10)**

1 Show that an analytic function is constant, if its real part is constant.

2 Evaluate  $\frac{1}{2\pi i} \int_C \frac{z^2 + 5}{z - 3} dz$  where  $C$  is  $|z| = 4$

3 Find the Taylor series expansion of  $f(z) = e^z$  at  $z = 0$

4 Determine the nature of singularity of the function  $f(z) = \frac{z - \text{Sin}z}{z^3}$

5 Find  $\nabla f$  where  $f(x, y, z) = x^2 + y^2 - 2z^2$  at  $(1, 1, 1)$

6 Find the velocity and acceleration at  $t=1/2$  of a moving particle whose position at time  $t$  is given by  $\vec{r}(t) = (t^2 + 1)i + (2t - 1)j$

7 Find the Fourier sine transform of  $2e^{-5x} + 5e^{-2x}$ .

**P.T.O**

**III****Answer ANY FIVE of the following****(5x4=20)**

①

1 ✓ Find the directional derivative of the function  $x^2y + yz + zx$  along the direction of  $i + 2j + 2k$  at the point  $(1, 2, 0)$ .

2 Show that  $\vec{F} = e^x(2y+3z)i + 2e^xj + 3e^xk$  is irrotational and find its scalar potential.

3 Find the Fourier Cosine transform of  $f(x) = \begin{cases} \cos x, & 0 < x < a \\ 0, & x > a \end{cases}$ .

4 Show that the function  $u = x^3 - 3xy^2$  is harmonic and find the analytic function whose real part is  $u$ .

5 Evaluate  $\int_C \frac{zdz}{(9-z^2)(z+i)}$  where  $C$  is the circle  $|z| = 2$  taken in the positive sense

② ✓ 6 Using residue theorem evaluate  $\int_C \frac{z^2 dz}{(z-2)(z+3)}$  where  $C$  is the circle  $|z| = 4$

③ ✓ Discuss the transformation  $w = e^z$

**IV****Answer ANY ONE of the following****(1x10=10)**

1 Expand  $f(z) = \frac{z}{(z-1)(2-z)}$  as a Laurent's series valid for

1)  $|z| < 1$     2)  $|z| > 2$     3)  $|z-1| > 1$     4)  $1 < |z| < 2$

2 Use Gauss divergence theorem to evaluate  $\iiint_S \vec{F} \cdot \hat{n} ds$  where  $S$  is the surface of rectangular parallelepiped  $0 \leq x \leq a, 0 \leq y \leq b, 0 \leq z \leq c$  and  $\vec{F} = x^2i + y^2j + z^2k$ .

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