## KERALA AGRICULTURAL UNIVERSITY <br> B.Tech.(Food Engg) 2016 Admission <br> IV Semester Final Examination-July 2018

Basc. 2209
Numerical Methods for Engineering Applications (1+1)
Marks: 50
Time:2hours

## I Fill up the following blanks:

1 In $\qquad$ method the values of $\mathrm{x}_{1}, \mathrm{x}_{2}, \ldots \ldots \ldots, \mathrm{x}_{\mathrm{n}}$ are obtained immediately without using back substitution.
2 Lagrange's interpolation formula is used only for $\qquad$ intervals.
3 One dimensional heat equation is $\qquad$ invals.
4 The positive root of $f(x)=2 x^{3}-3 x-6=0$ lies between
5. Iterative formula of Newton's Raphson method is

## State True or False

6 Newton-Raphson method is quadratically convergent.
7 Solution matrix of $\mathrm{AX}=\mathrm{B}$ by Gauss-elimination method is an upper triangular matrix.
8 Newton's forward interpolation formula is suitable to estimate the interpolations near the middle of the table value.
9 Modified Euler's method is the Runge-Kutta method of fourth order.
10 Error in the trapezoidal rule is of the order $h^{4}$.

## II Write Short notes on any FIVE of the following

1 Define interpolation and extrapolation.
2 i) Write trapezoidal rule.
ii) Write Newton's backward difference interpolation formula.

3 Classify the PDE $f_{x x}-2 f_{x y}=0$.
4 Using Gauss elimination method solve

$$
\begin{aligned}
& 2 x+y=3 \\
& 7 x-3 y=4
\end{aligned}
$$

5 Find relation between E and $\Delta$
6 Form the divided difference table for the following data

| x | 1 | 2 | 4 | 7 | 12 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{f}(\mathrm{x})$ | 22 | 30 | 82 | 106 | 206 |

7
Evaluate $\int_{0}^{1}\left(\frac{1}{1+x^{2}}\right) d x$ using Trapezoidal rule by taking interval $h=\frac{1}{2}$

## III Answer any FIVE of the following.

1 Solve the equation $x^{3}-2 x-5=0$ by Newton Raphson method.
2 Using Newton's forward interpolation formula find y at $x=8$ from the table:

| $x$ | 0 | 5 | 10 | 15 | 20 | 25 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 7 | 11 | 14 | 18 | 24 | 32 |

3 Find the value of $\int_{1}^{2}\left(\frac{1}{5+3 x}\right) \mathrm{dx}$ using Simpson's rule.
4. Obtain the values of $y$ at $x=0.1,0.2$ using R.K method of second order.

5 Solve $\frac{d y}{d x}=x+y$, given $y(1)=0$, and get $y(1.1)$ by Taylor series method.
6 Using Crank-Nicholson's method solve $u_{x X}=16 u_{t}, 0<x<1, t>0$ given $u(x, 0)=0, u(0, t)=0, u(1, t)=100 t$.Compute $u$ for one step in $t$ direction taking $\mathrm{h}=\frac{1}{4}$.
7 Write short notes on classification of partial differential equation of second order.

## IV Write Essay on ANY ONE

1. Explain briefly Gauss elimination and Gauss Jordan Methods.
2. The following are data from steam table.

| Temp $^{\circ} \mathrm{C}$ | 140 | 150 | 160 | 170 | 180 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Pressure $\mathrm{Kg} / \mathrm{cm}^{2}$ | 3.685 | 4.854 | 6.302 | 8.076 | 10.225 |

Using Newton's formula, find the pressure of the steam for a temperature of $142^{\circ} \mathrm{C}$.

