

KERALA AGRICULTURAL UNIVERSITY

B.Tech (Food.Engg.) 2016 Admission
1st Semester Final Examination-February-2017

Cat. No: Basc.1102.

Marks: 50.00

Title: Engineering Mathematics I (3+0)

Time: 2 hours

I Fill in the blanks/State True or False

(10x1=10)

1. The product of the eigenvalues of a matrix $A = \begin{bmatrix} 2 & -3 \\ 4 & -2 \end{bmatrix}$ is -----
2. Bending of a curve at a point is termed as ----- of a curve at that point.
3. If the rank of $A \neq$ rank of augmented matrix K , then the system of linear equations are -----
4. Define the chain rule for Jacobians.
5. Write the reduction formula for $\int \sin^n x dx$
6. If $y=0$ to 1 and $x=0$ to 3 , then evaluate $\iint (x^2 + 3y^2) dy dx$
7. Find the value of $\Gamma(1/2)$.
8. Write the parametric equation of a curve cycloid.
9. Write the condition for $f(x,y)$ to be maximum.
10. If $u = F(x-y, y-z, z-x)$, then find the value of $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} + \frac{\partial u}{\partial z} =$ -----

II Write short notes/answers on any FIVE of the following

(5x2=10)

1. Find the A^{-1} of a matrix $A = \begin{bmatrix} 1 & 4 \\ 2 & 3 \end{bmatrix}$
2. How to test the consistency of a system of equations in 'n' unknowns.
3. Using Cayley-Hamilton theorem, find the A^{-1} of $A = \begin{bmatrix} 1 & 4 \\ 2 & 3 \end{bmatrix}$
4. Expand $e^{\sin x}$ by Maclaurin's series up to terms containing x^4 .
5. Find the maximum and minimum values of $3x^4 - 2x^3 - 6x^2 + 6x + 1$ in the interval $(0,2)$.
6. If $u = x^3 + y^3 - 3axy$, then prove that $\frac{\partial^2 u}{\partial x \partial y} = \frac{\partial^2 u}{\partial y \partial x}$.
7. Change the order of integration of $\iint f(x,y) dy dx$, if the limits are $y=x$ to a and $x=0$ to a .

III Write short answers on any FIVE

(5x4=20)

1. Test whether the following system of equations has the trivial solution or not:
 $x+2y+3z=0, 3x+4y+4z=0, 7x+10y+12z=0$.
2. Let A be the square matrix of order 3 and $\lambda_1, \lambda_2, \lambda_3$ be its eigen values with eigen vectors X_1, X_2, X_3 respectively. Find its diagonal form $D = P^{-1} A P$.
3. Reduce the quadratic form $Q = 2xy + 2yz + 2zx$ into canonical form.
4. Expand e^x by Taylor's series in powers of $(x-1)$ up to 4th term.
5. Change the order of integration of $\iint f(x,y) dy dx$, if the limits are $y=x$ to \sqrt{x} and $x=0$ to 1 .
6. Find the radius of curvature at the point $(3a/2, 3a/2)$ of the Folium $x^3 + y^3 = 3axy$.

7. Verify Euler's theorem for $u = x^2yz - 4y^2z^2 + 2xz^3$.

IV Write essay on any ONE

(1x10=10)

1. Reduce the quadratic form $Q = 2x^2 + 2y^2 + 2z^2 - 2zx$ into canonical form by orthogonal transformation.
2. Change the order of integration and evaluate $\iint xy dx dy$, if the limits are $y=0$ to 1 and $x=x^2$ to $(2-x)$.
