

Sacs. 2110

Marks: 50
Time: 2 hours

## I Fill in the Blanks

$\qquad$
${ }^{2} \mathrm{~L}(\cos 4 \mathrm{t})=$ $\qquad$
$\Delta^{2} y_{2}=$
${ }^{4} \mathrm{~L}\left[y^{\prime}(t)\right]=$
$5^{\prime} \operatorname{COV}(\mathrm{X}, \mathrm{Y})=$ $\qquad$

## State True or False

6 The difference between the variances of two samples can be tested by chi Square test
7 The regression equations X on Y and Y on X meet at $(\bar{X}, \bar{Y})$
Mean and standard deviation of standard normal variate are 1 and 0
9 The type 1 error occurs when we rejects a true null hypothesis
The sum of deviations of the individual data elements from their mean is zero
II . Write Short notes on any FIVE of the following
Evaluate $\nabla x(x+1)$, taking $\mathrm{h}=1$
2
Write the Simpson's $1 / 3$ rule for $\int_{x_{0}}^{x_{0}+6 h} y d x$
3
Find $L^{-1}\left[\frac{s}{(s+2)^{2}+1}\right]$
Af Describe simple Euler's formula
Write the various measures of dispersion.
6 If $Q_{1}=7, Q_{2}=12$ and $Q_{3}=22$. Find the coefficient of quartile deviation.
If $\operatorname{COV}(\mathrm{X}, \mathrm{Y})=-6.8, \sigma_{X}=2.2$ and $\sigma_{Y}=3.4$, find the coefficient of correlation

A random sample of 100 farms in Punjab in a particular year gives an average yield of wheat 1400 lbs per acre with standard deviation of 62 lbs . Another random sample of 100 farms in the same year gives an average yield of 1260 lbs with a standard deviation 50 lbs . is the difference between average yields significant?
$\sqrt{2}$ Write the test procedure for finding the significance of difference between two population variances

3
Evaluate $\int_{0}^{1} \frac{\mathrm{dx}}{1+\mathrm{x}^{2}}$, using Trapezoidal rule with $\mathrm{h}=0.2$. hence determine the value of $\pi$
4 Using starlings formula to evaluate $y(1.22)$ given:

| x | 1.0 | 1.1 | 1.2 | 1.3 | 1.4 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{y}(\mathrm{x})$ | 0.841 | 0.891 | 0.932 | 0.963 | 0.985 |

5 Using Newton's divided difference formula, Find the cubic polynomial from the following table

| $x$ | 0 | 1 | 4 | 5 |
| :--- | :--- | :--- | :--- | :--- |
| $f(x)$ | 1 | 4 | $\cdots$ | 40 |



Given: $\frac{d y}{d x}+y=x^{2}, y(0)=1$, taking $h=0.1$. Determine $y(0.2)$ using modified Euler's method

Find the coefficient correlation between industrial production and export using the following data:

| Production (x) | 55 | 56 | 58 | 59 | 60 | 60 | 62 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Export (y) | 35 | 38 | 37 | 39 | 44 | 43 | 44 |

## IV Write an essay on any ONE of the following

1 Fit a poison distribution to the following data on number $(x)$ of bacterial colonies per culture plate in 445 culture plates (f). Calculate the theoretical frequencies and test their Goodness-of-fit.

| $x:$ | 0 | 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $f:$ | 264 | 117 | 42 | 15 | 7 |

$\int^{2}$ Solve $\frac{d x}{d t}+y=\sin t ; x+\frac{d y}{d t}=\cos t \quad$ with $\mathrm{x}=2$ and $\mathrm{y}=0$ when $\mathrm{t}=0$

